

**Statistics**  
**Spring 2023**  
**Lecture 44**



Feb 19-8:47 AM

40 randomly selected nurses had a mean salary of \$6250/mo.  $n=40, \bar{x}=6250$

It is known that standard deviation of salaries of all nurses is \$400/mo.  $\sigma=400$

Find Confidence Interval for the mean salaries of all nurses.  $\Rightarrow$  NO C-level  $\Rightarrow$  use 95%  $\mu$

Since  $\sigma$  is given  $\Rightarrow$  Z Interval

inpt: Stats

$\bar{x} = \frac{6374 + 6126}{2} = 6250$

$\sigma = 400$

$n = 40$

C-level: .95

Calculate

$6126 < \mu < 6374$

$E = \frac{6374 - 6126}{2} = 124$

May 3-7:21 AM

Find the minimum Sample Size needed if we wish to be 98% Confident and margin of error not to exceed \$100.

$E = Z_{\alpha/2} \cdot \frac{\sigma}{\sqrt{n}}$  with Some Algebra

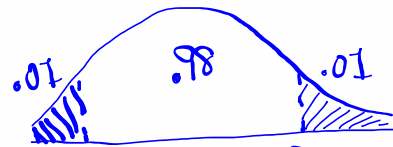
$$n = \left( \frac{Z_{\alpha/2} \cdot \sigma}{E} \right)^2$$

If decimal  $\rightarrow$  Round-up

$$n = \left( \frac{2.326 \cdot 400}{100} \right)^2$$

= 86.564

$n \approx 87$



= invNorm(.99, 0, 1) = 2.326

May 3-7:29 AM

32 randomly Selected exams had a mean of 86.5.  
 $n=32, \bar{x}=86.5$

It is known that standard deviation of Scores of all exams is 12.5.  $\sigma=12.5$

Find 90% Conf. interval for the mean Score of all exams. C-level: .9

$82.9 < \mu < 90.1$

Since  $\sigma$  is given  $\rightarrow$  Z Interval  
Since  $\bar{x}$  is in 1-decimal  $\rightarrow$  Round to 1-decimal

$$E = \frac{90.1 - 82.9}{2} = 3.6$$

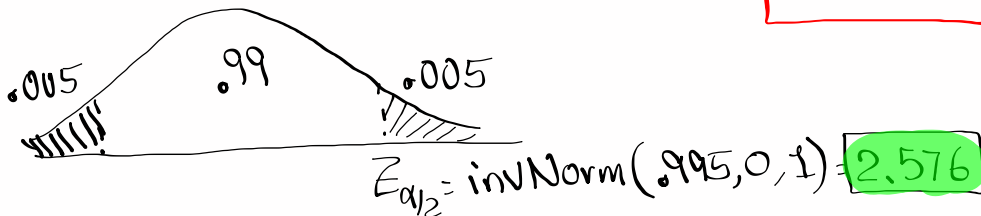
$$\bar{x} = \frac{90.1 + 82.9}{2} = 86.5$$

May 3-7:35 AM

find minimum Sample Size needed if we wish to construct 99% Conf. interval for the mean of all exams and error not to exceed 5 points.

$$n = \left( \frac{Z_{\alpha/2} \cdot \sigma}{E} \right)^2 = \left( \frac{2.576 \cdot 12.5}{5} \right)^2 = 41.4736$$

$n \approx 42$



May 3-7:42 AM

15 randomly selected cars on a certain FWY had a mean speed of 74 mph with standard deviation of 8 mph.

$$n = 15$$

$$\bar{x} = 74$$

$$s = 8$$

No C-level  $\rightarrow$  use 95%

find Conf. interval for the mean speed of all cars on that freeway.

$70 < \mu < 78$

$\sigma$  is not given  $\Rightarrow$  T Interval

$\bar{x}$  is a whole #  $\Rightarrow$  Round to whole #

$$E = \frac{78 - 70}{2} = 4$$

$$\bar{x} = \frac{78 + 70}{2} = 74$$

May 3-7:47 AM

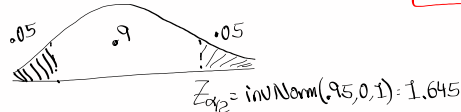
Find minimum Sample Size needed if we wish to construct 90% Conf. interval for the mean speed of all cars and error not to exceed 8 mph.

$$n = \left( \frac{Z_{\alpha/2} \cdot \sigma}{E} \right)^2$$

Since  $\sigma$  is not given, we use  $S$  instead

$$= \left( \frac{Z_{\alpha/2} \cdot S}{E} \right)^2 = \left( \frac{1.645 \cdot 8}{8} \right)^2 = 2.706$$

$n \approx 3$



Redo with  $E=5$

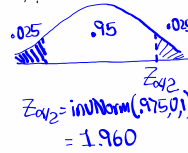
$$n = \left( \frac{1.645 \cdot 8}{5} \right)^2 = 6.927$$

$n = 7$

Redo with  $E=4$ , C-level: 95%

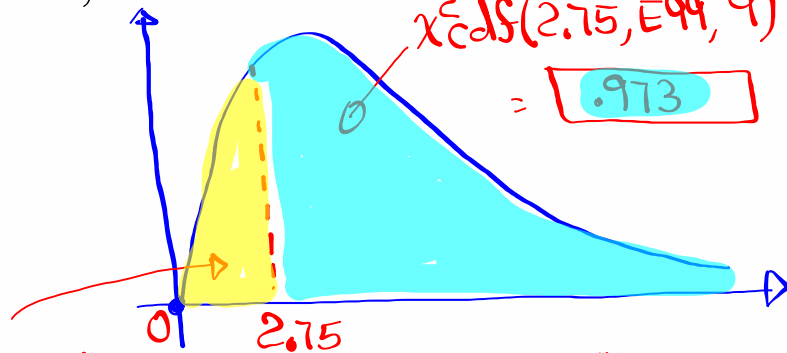
$$n = \left( \frac{1.960 \cdot 8}{4} \right)^2 = 15.3664$$

$n = 16$



May 3-7:55 AM

Find area on each side of  $\chi^2 = 2.75$  with  $df=9$ , then multiply the smaller area by 2.



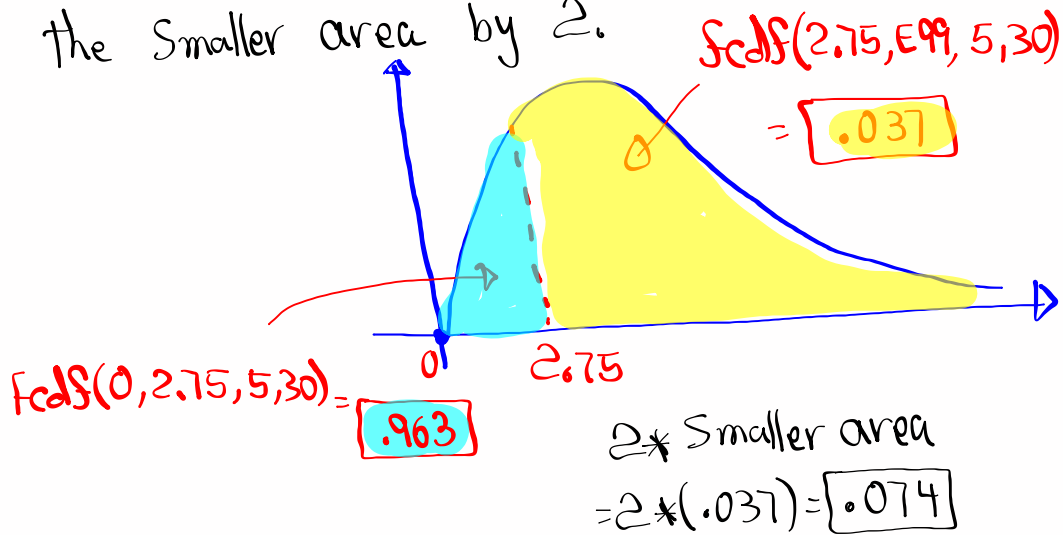
$\chi^2_{cdf}(0, 2.75, 9) = .027$

2 \* Smaller area  
= 2 (.027)

$= .054$

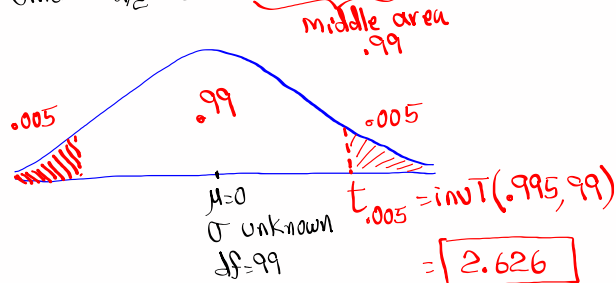
May 3-8:07 AM

find the area on each side of  $F=2.75$   
with  $Ndf=5$  &  $Ddf=30$ , then multiply  
the smaller area by 2.



May 3-8:12 AM

find  $t_{\alpha/2}$  for 99% c-level with  $df=99$ .



Redo with  $df=999$

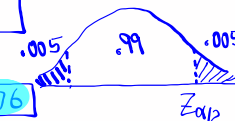
$\text{invT}(.995, 999) = 2.581$  (boxed)

Redo with  $df=9999$

$\text{invT}(.995, 9999) = 2.576$  (boxed)

Now find  $Z_{\alpha/2}$  for 99% c-level.

$Z_{\alpha/2} = \text{invNorm}(.995, 0, 1) = 2.576$  (boxed)



As  $df$  increase,  $t_{\alpha/2} \approx Z_{\alpha/2}$

May 3-8:16 AM